



Försättsblad till skriftlig tentamen vid Linköpings Universitet

Datum för tentamen	2011-04-27
Sal (1) Om tentan går i flera salar ska du bifoga ett försättsblad till varje sal och <u>ringa in</u> vilken sal som avses	KÅRA
Tid	14-18
Kurskod	TDDC17
Provkod	TEN1
Kursnamn/benämning Provnamn/benämning	Artificiell intelligens En skriftlig tentamen
Institution	IDA
Antal uppgifter som ingår i tentamen	8
Jour/Kursansvarig Ange vem som besöker salen	Mariusz Wzorek
Telefon under skrivtiden	0703887122
Besöker salen ca kl.	15.00
Kursadministratör/kontaktperson (namn + tfnr + mailaddress)	Anna Grabska Eklund, ankn. 2362, anna.grabska.eklund@liu.se
Tillåtna hjälpmedel	Miniräknare /Hand calculators.
Övrigt	
Vilken typ av papper ska användas, rutigt eller linjerat	valfritt
Antal exemplar i påsen	

Linköpings Universitet
Institutionen för Datavetenskap
Patrick Doherty

Tentamen
TDDC17 Artificial Intelligence
27 april 2011 kl. 14-18

Points:

The exam consists of exercises worth 37 points.
To pass the exam you need 18 points.

Auxiliary help items:

Hand calculators.

Directions:

You can answer the questions in English or Swedish.
Use notations and methods that have been discussed in the course.
In particular, use the definitions, notations and methods in appendices 1-3.
Make reasonable assumptions when an exercise has been under-specified.
Begin each exercise on a new page.
Write only on one side of the paper.
Write clearly and concisely.

Jourhavande: Mariusz Wzorek, 0703887122. Mariusz will arrive for questions around 15.00.

1. Consider the following theory (where x, y and z are variables and history, lottery and john are constants):

$$\forall x([Pass(x, history) \wedge Win(x, lottery)] \Rightarrow Happy(x)) \quad (1)$$

$$\forall x\forall y([Study(x) \vee Lucky(x)] \Rightarrow Pass(x, y)) \quad (2)$$

$$\neg Study(john) \wedge Lucky(john) \quad (3)$$

$$\forall x(Lucky(x) \Rightarrow Win(x, lottery)) \quad (4)$$

- (a) Convert formulas (1) - (4) into clause form. [1p]
 (b) Prove that $Happy(john)$ is a logical consequence of (1) - (4) using the resolution proof procedure. [2p]
- Your answer should be structured using a resolution refutation tree (as used in the book).
 - Since the unifications are trivial, it suffices to simply show the binding lists at each resolution step.
2. Constraint satisfaction problems consist of a set of variables, a value domain for each variable and a set of constraints. A solution to a CS problem is a consistent set of bindings to the variables that satisfy the constraints. A standard backtracking search algorithm can be used to find solutions to CS problems. In the simplest case, the algorithm would choose variables to bind and values in the variable's domain to be bound to a variable in an arbitrary manner as the search tree is generated. This is inefficient and there are a number of strategies which can improve the search. Describe the following three strategies:
- (a) Minimum remaining value heuristic (MRV). [1p]
 (b) Degree heuristic. [1p]
 (c) Least constraining value heuristic. [1p]

Constraint propagation is the general term for propagating constraints on one variable onto other variables. Describe the following:

- (d) What is the Forward Checking technique? [1p]
 (e) What is arc consistency? [1p]
3. Consider the following example:
- The fire alarm in a building can go off if there is a fire in the building or if the alarm is tampered with by vandels. If the fire alarm goes off, this can cause crowds to gather at the front of the building and fire trucks to arrive.*
- (a) Represent these causal links in a Bayesian network. Let a stand for "alarm sounds", c for "crowd gathers", f for "fire exists", t for "truck arrives", and v for "vandalism exists". [2p]
 (b) Given the independence assumptions implicit in the Bayesian network, what are the conditional (or prior) probabilities that need to be specified to fully determine the joint probability distribution? In other words, what are the conditional tables associated with each node? [2p]
 (c) Suppose there is a crowd in front of the building one day but that no fire trucks arrive. Given this, what is the probability that there is a fire, expressed as some function of the conditional (or prior) probabilities? [2p]
- Appendix 2 provides you with some help in answering these questions.

4. A* search is the most widely-known form of best-first search. The following questions pertain to A* search:

- (a) Explain what an *admissible* heuristic function is using the notation and descriptions in (c). [1p]
- (b) Suppose a robot is searching for a path from one location to another in a rectangular grid of locations in which there are arcs between adjacent pairs of locations and the arcs only go in north-south (south-north) and east-west (west-east) directions. Furthermore, assume that the robot can only travel on these arcs and that some of these arcs have obstructions which prevent passage across such arcs.

The *Manhattan distance* between two locations is the shortest distance between the locations ignoring obstructions. Is the Manhattan distance in the example above an admissible heuristic? Justify your answer explicitly. [2p]

- (c) Let $h(n)$ be the estimated cost of the cheapest path from a node n to the goal. Let $g(n)$ be the path cost from the start node n_0 to n . Let $f(n) = g(n) + h(n)$ be the estimated cost of the cheapest solution through n .

Provide a general proof that A* using tree-search is optimal if $h(n)$ is admissible. If possible, use a diagram to structure the proof. [2p]

5. Use the table below and the information in appendix 3 to answer the following questions pertaining to version spaces and the candidate elimination algorithm.

The following table shows a list of examples for a hypothetical credit-scoring application which might be used by a bank or credit-card company to filter prospective customers as to their credit worthiness. The target function is "person x is creditworthy".

Example	Age	Mortgage	Default	Length Employed	Surplus %	Creditworthy
1	18-60	No	No	1-5	No	Yes
2	18-60	Yes	No	1-5	No	Yes
3	< 18	No	No	< 1	No	No
4	18-60	No	Yes	1-5	No	No
5	18-60	No	No	> 5	No	Yes

Figure 1: Positive and negative training examples for Target Attribute Creditworthy

In the problem above *Creditworthy* is described in terms of the five attributes: Age, Mortgage (for house), Default (on loan), Length Employed, and Surplus (cash).

- (a) Is the Candidate-Elimination algorithm a supervised or unsupervised learning algorithm? Why?[1p]
- (b) Use the Candidate-Elimination algorithm to compute the version space containing all hypotheses from H (the space of hypotheses) that are consistent with the observed sequence of training examples in the table above for the target attribute *Creditworthy*. [4p]
- Initialize the algorithm with $G_0 = \{ \{?, ?, ?, ?, ?\} \}$ and $S_0 = \{ \langle \emptyset, \emptyset, \emptyset, \emptyset, \emptyset \rangle \}$
 - Provide a hand trace of the Candidate-Elimination algorithm learning from the training examples in the table above. In particular, show the specific and general boundaries of the version space after it has processed the first training example, the second training example, etc.

6. The following questions pertain to partial-order planning:

- (a) What is partial-order planning and how does it differ from STRIPS-based planning in terms of search space and output of the respective planning algorithms?[3p]
- (b) Describe the four basic components in a partial-order plan according to Russell/Norvig. [2p]

7. The following questions pertain to the course article by Newell and Simon entitled *Computer Science as an Empirical Enquiry: Symbols and Search*.
- (a) What is a *physical symbol system* (PSS) and what does it consist of? [2p]
 - (b) What is the Physical Symbol System Hypothesis? [1p]
8. Modeling actions and change in incompletely represented, dynamic worlds is a central problem in knowledge representation. The following questions pertain to reasoning about action and change.
- (a) What is Temporal Action Logic? Explain by describing the ontology used in the formalism, that is, what is taken to exist, and what notation is used in the logical language to represent those things that are taken to exist. [2p]
 - (b) What is the frame problem? Use the Wumpus world to provide a concrete example of the problem. Represent the problem by representing an initial timepoint, an action and the result of the action using the TAL notation (either with macros or without). [2p]
 - (c) What is nonmonotonic logic? How can it be used to provide solutions to the frame problem? [2p]

Appendix 1

Converting arbitrary wffs to clause form:

1. Eliminate implication signs.
2. Reduce scopes of negation signs.
3. Standardize variables within the scopes of quantifiers (Each quantifier should have its own unique variable).
4. Eliminate existential quantifiers. This may involve introduction of Skolem constants or functions.
5. Convert to prenex form by moving all remaining quantifiers to the front of the formula.
6. Put the matrix into conjunctive normal form. Two useful rules are:
 - $\omega_1 \vee (\omega_2 \wedge \omega_3) \equiv (\omega_1 \vee \omega_2) \wedge (\omega_1 \vee \omega_3)$
 - $\omega_1 \wedge (\omega_2 \vee \omega_3) \equiv (\omega_1 \wedge \omega_2) \vee (\omega_1 \wedge \omega_3)$
7. Eliminate universal quantifiers.
8. Eliminate \wedge symbols.
9. Rename variables so that no variable symbol appears in more than one clause.

Appendix 2

A generic entry in a joint probability distribution is the probability of a conjunction of particular assignments to each variable, such as $P(X_1 = x_1 \wedge \dots \wedge X_n = x_n)$. The notation $P(x_1, \dots, x_n)$ can be used as an abbreviation for this.

The chain rule states that any entry in the full joint distribution can be represented as a product of conditional probabilities:

$$P(x_1, \dots, x_n) = \prod_{i=1}^n P(x_i \mid x_{i-1}, \dots, x_1) \quad (5)$$

Given the independence assumptions implicit in a Bayesian network a more efficient representation of entries in the full joint distribution may be defined as

$$P(x_1, \dots, x_n) = \prod_{i=1}^n P(x_i \mid \text{parents}(X_i)), \quad (6)$$

where $\text{parents}(X_i)$ denotes the specific values of the variables in $\text{Parents}(X_i)$.

Recall the following definition of a conditional probability:

$$\mathbf{P}(X \mid Y) = \frac{\mathbf{P}(X \wedge Y)}{\mathbf{P}(Y)} \quad (7)$$

The following is a useful general inference procedure:

Let X be the query variable, let \mathbf{E} be the set of evidence variables, let \mathbf{e} be the observed values for them, let \mathbf{Y} be the remaining unobserved variables and let α be the normalization constant:

$$\mathbf{P}(X \mid \mathbf{e}) = \alpha \mathbf{P}(X, \mathbf{e}) = \alpha \sum_{\mathbf{y}} \mathbf{P}(X, \mathbf{e}, \mathbf{y}) \quad (8)$$

where the summation is over all possible \mathbf{y} 's (i.e. all possible combinations of values of the unobserved variables \mathbf{Y}).

Equivalently, without the normalization constant:

$$\mathbf{P}(X \mid \mathbf{e}) = \frac{\mathbf{P}(X, \mathbf{e})}{\mathbf{P}(\mathbf{e})} = \frac{\sum_{\mathbf{y}} \mathbf{P}(X, \mathbf{e}, \mathbf{y})}{\sum_{\mathbf{x}} \sum_{\mathbf{y}} \mathbf{P}(\mathbf{x}, \mathbf{e}, \mathbf{y})} \quad (9)$$

Appendix 3

Begin: Candidate-Elimination Learning Algorithm

Initialize G to the set of maximally general hypotheses in H

Initialize S to the set of maximally specific hypotheses in H

For each training example d , do

- If d is a positive example
 - Remove from G any hypothesis inconsistent with d
 - For each hypothesis s in S that is not consistent with d
 - * Remove s from S
 - * Add to S all minimal generalizations h of s such that
 - h is consistent with d , and some member of G is more general than h
 - * Remove from S any hypothesis that is more general than another hypothesis in S
- If d is a negative example
 - Remove from S any hypothesis inconsistent with d
 - For each hypothesis g in G that is not consistent with d
 - * Remove g from G
 - * Add to G all minimal specializations h of g such that
 - h is consistent with d , and some member of S is more specific than h
 - * Remove from G any hypothesis that is less general than another hypothesis in G

End: Candidate-Elimination Learning Algorithm

Hypothesis representation: Let each hypothesis be a vector of n constraints, specifying the values of each of the n attributes in a problem. For each attribute, the hypothesis will either

- indicate by a "?" that any value is acceptable for this attribute,
- specify a single required value for the attribute
- indicate by a "∅" that no value is acceptable.

Definition 1

A hypothesis h is consistent with a set of training examples D if and only if $h(x) = c(x)$ for each example $(x, c(x))$ in D .¹

$$\text{Consistent}(h, D) \equiv (\forall (x, c(x)) \in D) h(x) = c(x).$$

Definition 2

The **general boundary** G , with respect to hypothesis space H and training data D , is the set of maximally general members of H consistent with D .²

$$G \equiv \{g \in H \mid \text{Consistent}(g, D) \wedge (\neg \exists g' \in H)[(g' >_g g) \wedge \text{Consistent}(g', D)]\}$$

Definition 3

The **specific boundary** S , with respect to hypothesis space H and training data D , is the set of minimally general (i.e., maximally specific) members of H consistent with D .

$$S \equiv \{s \in H \mid \text{Consistent}(s, D) \wedge (\neg \exists s' \in H)[(s >_g s') \wedge \text{Consistent}(s', D)]\}$$

¹Here, x is an example, h is a hypothesis returning true or false and c is the target concept returning true or false.

² $h >_g h'$ states that h is strictly more general than h' . $h_j \geq_g h'_j$ if and only if: $\forall (x \in X)[(h_k(x) = 1) \rightarrow (h'_j(x) = 1)]$.