

Table with common formulas and moment generating functions

Some common mathematical results

$$\begin{aligned} e^x &= \sum_{n=0}^{\infty} \frac{x^n}{n!} \\ e^x &= \lim_{n \rightarrow \infty} \left(1 + \frac{x}{n}\right)^n \\ \sum_{k=0}^{n-1} ar^k &= a \frac{1-r^n}{1-r} \quad \text{if } r \neq 1 \\ \sum_{k=0}^{\infty} ar^k &= \frac{a}{1-r} \quad \text{if } |r| < 1 \\ (x+y)^n &= \sum_{k=0}^n \binom{n}{k} x^k y^{n-k} \end{aligned}$$

Moment generating functions for some common distributions

Distribution	Abbreviation	Moment generating function
Bernoulli	$Be(p)$	$q + pe^t$
Binomial	$Bin(n, p)$	$[q + pe^t]^n$
Poisson	$Po(m)$	$e^{m(e^t - 1)}$
Uniform	$U(a, b)$	$\frac{e^{tb} - e^{ta}}{t(b-a)}$
Exponential	$Exp(a)$	$\frac{1}{1-at}$ for $t < 1/a$
Gamma	$\Gamma(p, a)$	$\frac{1}{(1-at)^p}$ for $t < 1/a$
Laplace	$L(a)$	$\frac{1}{1-a^2 t^2}$ for $ t < 1/a$
Normal	$N(\mu, \sigma^2)$	$e^{t\mu + \sigma^2 t^2/2}$

Some statistical results

$Y|X = x \sim N \left[\mu_y + \rho \frac{\sigma_y}{\sigma_x} (x - \mu_x), \sigma_y^2 (1 - \rho^2) \right]$ if Y and X are jointly normal.

$\vec{Y}|\vec{X} = \vec{x} \sim N \left[\vec{\mu}_y + \boldsymbol{\Sigma}_{yx} \boldsymbol{\Sigma}_{xx}^{-1} (\vec{x} - \vec{\mu}_x), \boldsymbol{\Sigma}_{yy} - \boldsymbol{\Sigma}_{yx} \boldsymbol{\Sigma}_{xx}^{-1} \boldsymbol{\Sigma}_{xy} \right]$ if Y and X are jointly normal.