# CHALMERS UNIVERSITY OF TECHNOLOGY 

## Department of Energy and Environment

Electric Drives 1 (ENM055)
Re-Examination
Thursday 17 January 2013, 14:00-18:00

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| Grading: | Your score from this written examination (maximum 70 points) will be <br> added to your points obtained from laboratory work (maximum 30 <br> points) and from the trial exam (maximum 10 points). The grading will <br> then be as follows: |

50-64 points G3 $\quad 65-79$ points G4 $>79$ points G5
Solutions: $\quad$ Solutions will be put on the course home page after the exam.

Use of approved calculators (refer to the University's Examination Regulations) is allowed.

Use of Dictionaries and basic mathematics and physics handbook is allowed.

If there is any missing information in the following questions, you can make reasonable assumptions and state them clearly.

## Good Luck

1. A separately excited dc motor runs from 300 V supply and draws an armature current of 20 A at a field current 2 A . The armature resistance is $2 \Omega$. If the field current is suddenly reduced to 1.5 A , calculate the value to which the armature current reaches momentarily.

## [10 points]

2. The full-load slip of an 4-pole induction motor at 50 Hz is 0.04 . Estimate the speed if:
a) the frequency is reduced to 25 Hz keeping $\mathrm{U} / \mathrm{f}=$ constant and the torque constant b) the frequency is increased to 75 Hz , .keeping the same voltage as in the 50 Hz case and reducing the load torque to $50 \%$
[10 points]
3. Figure Q 3 shows a cross section area of a three-phase ac motor. The aim of the question is to calculate the net magnetic flux in the air-gap, $\Phi$. Assume that the three-phase currents are flowing in the windings as follows:
$i_{a \dot{a}}(t)=I_{M} \sin \omega t$
$i_{b \tilde{b}}(t)=I_{M} \sin \left(\omega t-\frac{2 \pi}{3}\right)$
$i_{c \dot{c}}(t)=I_{M} \sin \left(\omega t+\frac{2 \pi}{3}\right)$
Assume that the resulted mmf is sinusoidally distributed in the air gap and is proportional with the currents for each phase. Calculate the total magnetic flux in the air-gap $\Phi$ expressed as a function of the amplitude of the flux from one phase, $\Phi_{\mathrm{M}}$. (there is no saliency in the rotor and materials are ideal).


Figure Q3. Cross section area of a stator with three-phase windings
4. a) A 4-phase switched reluctance motor has 8 stator poles and 6 rotor poles, see Fig. Q4 where the coils of phase 1 is shown (but not the coils of phase 2,3, and 4). Draw the phase 1 inductance versus rotor position if the stator pole angle is $20^{\circ}$ and the rotor pole angle is $25^{\circ}$. The inductance at the aligned position is $L_{a}$ and the inductance at the unaligned position is $L_{u}$. Draw also the phase 1 current as a function of rotor position. How many times should the phase 1 current be switched on during one rotor revolution $\left(360^{\circ}\right)$ ?
a) Give one advantage and one disadvantage with the Switched Reluctance motor drive compared to a synchronous motor drive.


Figure Q4. The stator, rotor and the phase 1 coils of a 4-phase SR motor
5. Consider a synchronous generator with following specifications:

- Phase voltage: 480 Vrms in Y
- Nominal frequency: 60 Hz
- Synchronous Reactance per phase: 1 Ohm
- Number of poles: 6

The armature full current is 60 A in power factor (PF) 0.8 lag . Moreover, in full load condition the mechanical loss is 1.5 kW and core loss is 1 kW . Assume that copper losses are negligible. The field current is adjusted to have a terminal voltage of 480 V in the no load condition. Answer to the following questions:
a) What is the generator speed?
b) What is the terminal voltage in following conditions? Draw a phasor diagrams in each case also.
b1) Full load current with $\mathrm{PF}=0.8 \mathrm{lag}$
b2) Full load current with $\mathrm{PF}=1$
b3) Full load current with $\mathrm{PF}=0.8$ lead
c) What is the efficiency of the generator in full load current while $\mathrm{PF}=0.8$ lag?
[10 points]
6. A 4-pole brushless-dc motor with surface mounted permanent magnets has a rating of 2 kW and 2000 rpm . The per phase resistance is $0.5 \Omega$ and the per phase induced voltage is 120 V
a) Draw the equivalent circuit of the BLDC motor and calculate the value of the parameters used (the inductance can in this case be neglected)
b) Calculate the rated torque at 1000 rpm (do reasonable assumptions)
c) Calculate the maximum no load speed of the motor if the available DC-bus voltage is 280 V
d) Calculate the instantaneous peak torque at zero speed (neglect any thermal issues that this might cause). Is the result you obtain realistic? Motivate your answer!
[15 points]
7. You are about to pick a motor to certain application where you have decided that the induction motor and the PMSM motor is the best candidates. State the main advantages and disadvantage between the two candidates.
[5 points]

## Solutions:

## Problem 1:

Dc-motor, $\mathrm{Ua}=300 \mathrm{~V}, \mathrm{Ra}=2 \Omega$, La is assumed zero, $\mathrm{Ia}=20 \mathrm{~A}$ at $\mathrm{If}=2 \mathrm{~A}$ gives that $\mathrm{Ea}=\mathrm{Ua}-\mathrm{Ra} * \mathrm{Ia}=300-20 * 2=260 \mathrm{~V}$.

Then, field current If is reduced to If2=1.5 A and Ea reduce instantaneously a factor (If/If2) while speed change slowly due to inertia. Thus,
$\mathrm{Ea}=300 /(2 / 1.5)=225 \mathrm{~V}$
Then $\mathbf{I a}=(\mathrm{Ua}-\mathrm{Ea}) / \mathrm{Ra}=\mathbf{3 7 . 5} \mathbf{A}$
(This flux reduction gives increased speed as supplied voltage is constant and flux is proportional to Ua/frequency. Initially, the increased armature current gives increased torque. Then, as speed increase, Ea increase and Ia reduce)

## Problem 2:

a) Voltage is adjusted to maintain full air gap flux, so voltage decrease as frequency decrease.
Rotor resistance is assumed constant and core loss is ignored.
$\mathrm{p}=4$ (number of poles)
$\mathrm{Sn}=0.04$
$\mathrm{f}=50 \mathrm{~Hz}$
$\mathrm{f}=25 \mathrm{~Hz}$
For frequencies of 50, 25 corresponding synchronous speeds for the 2-pole machine are:
$\mathrm{n}_{\mathrm{s}}=(2 / \mathrm{p}) * \mathrm{f} * 60=1500 \mathrm{rpm}$
$\mathrm{n}_{\mathrm{s}^{\prime}}=(2 / \mathrm{p}) * \mathrm{f}^{\prime} * 60=750 \mathrm{rpm}$
slips in rpm are not changing so the slip can be calculated as
slip $=0.04 * 1500=60 \mathrm{rpm}$
The rated speed at 25 Hz can now be calculated as
$\mathrm{n}=750-60=690 \mathrm{rpm}$
b) The frequency is now increased to 75 Hz keeping the same voltage. Hence the flux in the machine will decrease as follows
$\Phi \sim \mathrm{U} / \mathrm{f}$
$\Phi_{2} / \Phi_{1} \sim \mathrm{f}_{1} / \mathrm{f}_{2}=50 / 75=2 / 3$
In order to produce $50 \%$ of the rated flux at 75 Hz it the slip will be higher than 30 rpm (which would be that case at rated flux). We need to compensate for the fact that the flux has reduced
and that the induced current in the rotor has reduced. Hence the new slip can be calculated from the synchronous speed ( 2250 rpm ) as follows
$\operatorname{slip}_{75 \mathrm{~Hz}}=(30 / 2250) /(2 / 3)^{2}=0.03$
Finally the speed can be calculated as
$2250-2250 * 0.03=2182.5 \mathrm{rpm}$

## Problem 3

- The three phase load currents produce a rotating flux with constant amplitude.

The produced magnetic flux can be written as:

$$
\begin{aligned}
& \Phi_{a \dot{a}}(t)=\Phi_{M} \sin \omega t<0^{\circ} \\
& \Phi_{b \bar{b}}(t)=\Phi_{M} \sin \left(\omega t-\frac{2 \pi}{3}\right)<\frac{2 \pi}{3} \\
& \Phi_{c \dot{c}}(t)=\Phi_{M} \sin \left(\omega t+\frac{2 \pi}{3}\right)<\frac{4 \pi}{3}
\end{aligned}
$$

The amplitude of the total flux is calculated at time $t=0$ at a point on the magnetic axis of a'a:

$$
\begin{aligned}
& \Phi(t)=\Phi_{a \dot{a}}(t=0)<0^{o}+\Phi_{b \dot{b}}(t=0)<\frac{2 \pi}{3}+\Phi_{c \dot{c}}(t=0)<\frac{4 \pi}{3}= \\
& 0+\Phi_{M} \sin \left(-\frac{2 \pi}{3}\right)<\frac{2 \pi}{3}+\Phi_{M} \sin \left(\frac{2 \pi}{3}\right)<\frac{4 \pi}{3}=\cdots=1.5 \Phi_{M}<-\frac{\pi}{2}
\end{aligned}
$$

For an arbitrary point in the stator periphery, the phase shift is compensated by the angle as well.

## Problem 4

a) A 4-phase switched reluctance motor has 8 stator poles and 6 rotor poles, see Fig. 1 where the coils of phase 1 is shown (but not the coils of phase 2,3, and 4). Draw the phase 1 inductance versus rotor position if the stator pole angle is $20^{\circ}$ and the rotor pole angle is $25^{\circ}$. The inductance at the aligned position is $\mathrm{L}_{\mathrm{a}}$ and the inductance at the unaligned position is $\mathrm{L}_{\mathrm{u}}$. Draw also the phase 1 current as a function of rotor position. How many times should the phase 1 current be switched on during one rotor revolution $\left(360^{\circ}\right)$ ?
b) Give one advantage and one disadvantage with the Switched Reluctance motor drive compared to a synchronous motor drive.

## Solution:

$\beta_{\mathrm{s}}=20^{\circ}$, stator gap $=25^{\circ}, \beta_{\mathrm{r}}=25^{\circ}$, rotor gap $=35^{\circ}, 8$ stator poles and 6 rotor poles


Current should be switched on 6 times per revolution.
c) Example of advantages: Low cost, fault tolerant. Example of disadvantages: Low efficiency, noisy.

## Problem 5

The generator is Y connected and the Phase voltage, $\mathrm{V}_{\varphi}$, is: $V_{\varphi}=\frac{V_{T}}{\sqrt{3}}=277 v$ where $\mathrm{V}_{\mathrm{T}}$ is terminal voltage that is 480 v in this case. Since the terminal voltage is adjusted in no load condition, it will be generator internal voltage without armature reaction. So the internal voltage is $E_{A}=277 \mathrm{v}$.
a) The generator mechanical speed can be calculated as: $n_{m}=\frac{120 f_{e}}{P}=1200 \mathrm{rpm}$.
b) The phasor diagram is shown in the following diagram for different cases consequently. The figure shows how to calculate the voltage by using the triangle.
The voltage equation is:

$$
E_{A}=V_{\varphi}+j I_{A} X_{S}
$$

where $\mathrm{I}_{\mathrm{A}}$ is phase current and $\mathrm{X}_{\mathrm{s}}$ is synchronous reactance. The phase voltage, $V_{\varphi}$, is the reference vector, a phasor with 0 angle. The current angle is known from the PF. So the unknowns are the internal voltage angle that is $\delta$ and the phase voltage magnitude $V_{\varphi}$.

1) $E_{A}^{2}=\left(V_{\varphi}+X_{S} I_{A} \sin \theta\right)^{2}+\left(X_{S} I_{S} \cos \theta\right)^{2} \rightarrow V_{\varphi}=236.8 v \rightarrow V_{T}=410 v$
2) $V_{T}=468.4 v$ and $V_{\varphi}=270 v$
3) $V_{T}=535 v$ and $V_{\varphi}=309 v$
c) In $\mathrm{PF}=0.8$ lag and $\mathrm{I}_{\mathrm{A}}=60$ A the output power is: $P_{\text {out }}=\sqrt{3} V_{T} I_{A} \cos \theta=3 V_{\varphi} I_{A} \cos \theta=39.9$ kW .
The input power that is mechanical power can be written as:
$P_{\text {in }}=P_{\text {out }}+P_{\text {elec loss }}+P_{\text {core loss }}+P_{\text {mech loss }}=33.9 \mathrm{~kW}+0+1 \mathrm{~kW}+1.5 \mathrm{~kW}=42.4 \mathrm{~kW}$
Efficiency is $\eta=\frac{P_{\text {out }}}{P_{\text {in }}}=\frac{39.9}{42.4} \times 100=94.1 \%$


## Problem 6

Eq circuit sees course material
The task gave us numbers of the per phase resistance and induced voltage. However, the eq. circuit of the BLDC motor represents two phases in series so the resistance will be $1 \Omega$ and the induced voltage 240 V
b) We can assume that the rated torque is the same for 1000 rpm as it is at 2000rpm. Hence the rated torque can be calculated as
$\mathrm{T}=\mathrm{P} / \omega=2000 /(2000 \pi /(30)=9.55 \mathrm{Nm}$
c) The available voltage is 280 V and we can assume that the maximum speed will be reached when the induced voltage is 280 . Hence the maximum speed can be calculated as
$\max$ speed $=280 / 240 * 2000=2333 \mathrm{rpm}$
d) If we neglect any thermal or saturation issues we can assume that the output torque is proportional to the current. At zero speed (zero induced voltage) we get a current of $\mathrm{I}=280 / 1=280 \mathrm{~A}$.

We also know the induced voltage at rated operation so we can calculate the motor contant and the current that provides rated torque
$\mathrm{Ke}=\mathrm{Ea} / \mathrm{wr}=240 /(2000 \pi / 30)=1.146$
$\mathrm{I}=\mathrm{T} / \mathrm{ke}=9.55 / 1.146=8.33 \mathrm{~A}$

The torque zero speed can now be calculated as:
$9.55 / 8.33 * 280=320 \mathrm{Nm}$

NOTE that this is not realistic in practice since we will reach saturation in the iron long before this..

## Problem 7

If we compare the two motor types:
PMSM: + efficiency

+ power density
- Cost
- robustness

IM: $\quad+$ Cost
+Robustness
-efficiency
-power density

