## DAT105 - COMPUTER ARCHITECTURE.

EXAM SOLUTIONS FOR 2009-12-17

## Assignment 1.

A)
(i) $\mathrm{T}_{\mathrm{A}}=(1+2+4) / 3=2.3 ; \mathbf{T}_{\mathbf{B}}=(\mathbf{2}+\mathbf{2}+\mathbf{2}) / \mathbf{3}=\mathbf{2} ; \mathrm{T}_{\mathrm{R}}=(6+1+1) / 3=2.7$
$B$ have the highest performance when using arithmetic mean.
Using arithmetic mean to compare programs results in that programs with longer execution times impacts the result higher than programs with shorter execution times.
(ii), (iii) :

|  | Comp A | Comp B | Ref comp |
| :--- | :--- | :--- | :--- |
| P1/R | $1 / 6$ | $2 / 6$ | 1 |
| P2/R | 2 | 2 | 1 |
| P3/R | 4 | 2 | 1 |
|  |  |  |  |
| Geometric <br> mean | 1.1 | 1.1 | 1 |

A \& B have the same performance when using the geometric mean of the normalized execution times.

## B.

Amdahl's law : SpeedUp $_{\text {overall }}=1 /(1-\mathrm{F}+\mathrm{F} / \mathrm{S})$; where $\mathrm{F}=$ Fraction of the total time that can be sped up. $\mathrm{S}=$ Speedup factor (=no. of processors)

$$
\text { SpeedUp }_{\text {overall }}=1 /(1-0.8+0.8 / \mathrm{S})=1 /(0.2+0.8 / \mathrm{S}) ;
$$

Let S -> infinity: SpeedUp ${ }_{\text {overall }}$-> $1 / 0.2=5$.
C.

$$
\begin{aligned}
& \mathbf{T}_{\text {exe }}=\mathbf{I C} * \mathbf{C P I}_{\text {ave }} * \mathbf{T}_{\mathbf{c}} \\
& \mathrm{CPI}_{\text {ave }}=\mathrm{CPI}_{\text {base }} * 0.8+\mathrm{CPI}_{\text {memrefs }} * 0.2=1 * 0.8+2 * 0.2=1.2 \\
& \mathrm{~T}_{\text {exe }}=10^{9} * 1.2 * 10^{-9}=1.2 \text { seconds }
\end{aligned}
$$

## Assignment 2.

A)
(i)
$\begin{array}{lll}\text { LOOP: } & \text { LD } & \\ \text { DMUL } & \text { R5, } \mathrm{R} 4, \mathrm{R} 4 & \text { RAW dependence on } \mathrm{R} 4^{1} \\ \text { SD } & \text { R5, } 0(\mathrm{R} 1) & \text { RAW dependence on } \mathrm{R} 5^{2} \\ \text { DADDI } & \mathrm{R} 1, \mathrm{R} 1,8 & \\ \text { BNE } & \mathrm{R} 1, \mathrm{R} 2, \text { LOOP } & \text { RAW dependence on } \mathrm{R} 1^{3}\end{array}$

Assuming a 5-stage pipeline structure using forwarding/bypass for handling of RAW hazards (shown as red thick arrows):

(ii) See execution diagram in (iii)
$1{ }^{\text {st }}$ RAW: Partly resolved via forward MEM -> EXE/MUL1
$2{ }^{\text {nd }}$ RAW: Partly resolved via forward MEM/MUL2 -> EXE
$3^{\text {rd }}$ RAW: Resolved via forward EXE -> EXE
(iii) Control hazard (branch delay slots) $=2 ;$ RAW $=2$ stall cycles.

| Cycle No. | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| LD R4,0(R1) | IF | ID | EXE | MEM | WB |  |  |  |  |  |  |
| DMUL R5,R4,R4 |  | IF | ID | stall | MUL1 | MUL2 | WB |  |  |  |  |
| SD R5,0(R1) |  |  | IF | stall | ID | stall | EXE | MEM | WB |  |  |
| DADDI R1,R1,8 |  |  |  |  | IF | stall | ID | EXE | MEM | WB |  |
| BNE R1,R2,LOOP |  |  |  |  |  |  | IF | ID | EXE | MEM | WB |
| Delay slot 1 |  |  |  |  |  |  |  | IF | ID | EXE | $\ldots .$. |
| Delay slot 2 |  |  |  |  |  |  |  |  | IF | ID | $\ldots .$. |

Number of cycles per vector element is 9 cycles.
B) Assume n is an even number. Then unroll the loop once and put "NOP" in the delay slots.

| LOOP: | LD | R4, 0(R1) |  |
| :--- | :--- | :--- | :--- |
|  | DMUL | R5, R4, R4 |  |
|  | SD | R5, 0(R1) |  |
|  | DADDI | R1, R1, 8 | delay slot |
| delay slot |  |  |  |
| NOP |  |  |  |
| NOP |  |  |  |
|  |  |  |  |
| LD | R4, 0(R1) |  |  |
| DMUL | R5, R4, R4 | delay slot |  |
| SD | R5, 0(R1) | delay slot |  |

Now, move the second LD up, the second SD down, merge the two DADDI's, adjust offsets, and rename R4 and R5 :

LOOP: LD R4, 0(R1)
LD $\quad$ R3, 8(R1)

DMUL R5, R4, R4
DMUL R6, R3, R3

DADDI R1, R1, 16
BNE R1, R2, LOOP

SD R5,-16(R1)
SD R6,-8(R1)

R5 renamed to R6
R4 renamed to R3

R5 renamed to R6

| Cycle No. | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| LD R4,0(R1) | IF | ID | EXE | MEM | WB |  |  |  |  |  |  |  |
| LD R R3,8(R1) |  | IF | ID | EXE | MEM | WB |  |  |  |  |  |  |
| DMUL R5,R4,R4 |  |  | IF | ID | MUL1 | MUL2 | WB |  |  |  |  |  |
| DMUL R6,R3,R3 |  |  |  | IF | ID | MUL1 | MUL2 | WB |  |  |  |  |
| DADDI R1,R1,16 |  |  |  |  | IF | ID | EXE | MEM | WB |  |  |  |
| BNE R1,R2,LOOP |  |  |  |  |  | IF | ID | EXE | MEM | WB |  |  |
| SD R5,-16(R1) |  |  |  |  |  |  | IF | ID | EXE | MEM | WB |  |
| SD R6,-8(R1) |  |  |  |  |  |  |  | IF | ID | EXE | MEM | WB |

(i) Two times (assuming n is even)
(ii) Two rename registers (R3 and R6)
(iii) New loop has 8 instructions so each loop now has 3 more instructions.

However, since two vector elements are now computed in 8 cycles the number of cycles per vector element is reduced to 4 cycles.
C) In the C assignment we do not use loop unrolling but just reschedule the code within one loop iteration. To reduce control hazards we can move the SD instruction down into one of the delay slots. One cycle is then lost due to control hazard :

LOOP: LD R4, 0(R1)
DMUL R5, R4, R4
DADDI R1, R1, 8
BNE R1, R2, LOOP
SD R5,-8(R1)
NOP Delay slot

Note. Moving also the DMUL instruction into the delay slots will not help since then we would have an RAW hazard on R5 which is not solved by forwarding.
D) See book pages 82-83 and Figure 2.4. We would have one entry corresponding to the BNE instruction in the end of the program. The prediction would evolve according to this table if we assume we start in state 00 and assuming $n>5$ :

| Execution <br> of BNE <br> instruction | Prediction <br> state be- <br> fore exec | 00 | Prediction |
| :--- | :--- | :--- | :--- |
| first | 01 | Not taken <br> (wrong) <br> after <br> exec |  |
| second | 11 | Not taken <br> (wrong) | (it <br> was <br> taken) |
| third | 11 | Taken <br> (correct) | 11 (it <br> was <br> taken) |
| $4^{\text {th }, 5^{\text {th }}, \text { etc }}$ | Taken <br> (correct) | 11 (it <br> was <br> taken) |  |
| Iteration $n$ | Not taken <br> (wrong) | (it <br> was <br> taken) |  |

## CHALMERS

## Assignment 3.

| A) SUB F0, F1, F2 |  |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| DIV ADD |  |  |  |  | WAR name dependence on F4 |  |  |  |  |  |  |
| The three stages of Tomasulo's Algorithm : |  |  |  |  |  |  |  |  |  |  |  |
| - Issue instruction if no structural hazard for a reservation station <br> - Read already available operands |  |  |  |  |  |  |  |  |  |  |  |
| - Execute when both operands are available; if operad(s) not ready, watch Common Data Bus (CDB) for result |  |  |  |  |  |  |  |  |  |  |  |
| - Write on CDB to all awaiting functional units; <br> - Mark reservation station available. |  |  |  |  |  |  |  |  |  |  |  |
| B) |  |  |  |  |  |  |  |  |  |  |  |
| Cycle \#: | 12 | 3 | 4 | 5 . | 9 | 10 | 11 |  | .... | 19 | 20 |
| SUB | I EX | EX | EX | .... | EX | WR |  |  |  |  |  |
| DIV | I |  |  | $\ldots$ |  | EX | EX | EX | .... | EX | WR |
| ADD |  |  | EX | EX ... | EX | WR |  |  |  |  |  |

The last instruction (ADD) write to the register file in cycle \#10.

## C)

The four steps of a Speculative Tomasulo algorithm:

## 1. Issue

- If reservation station and reorder buffer slot free, issue instr \& send operands \& reorder buffer nr. for destination

2. Execution

- If both operands ready: execute; if not, watch CDB for result;
when both operands are in reservation station: execute

3. Write result

- Write on Common Data Bus to all awaiting FUs \& reorder buffer; mark reservation station available

4. Commit - update register with reorder result

- When instr. is at head of reorder buffer \& result is present; update register with result (or store to memory) and remove instr. from reorder buffer
D) F0 is supplied via the CDB bus (in cycle \#10 in the example above).


## Assignment 4.

## A)

Compulsory (or cold) miss: The first reference to a block is always a miss.
Capacity miss: If the space is not sufficient to host the data or code that have been accessed.
Conflict miss: Two memory blocks may be mapped to the same cache block with a direct or setassociative address mapping even if there is still unused space in cache.

## B)

Average memory access time $=$ Hit time + Miss rate x Miss penalty .

## C)

Way prediction addresses "Hit time". Used in Set-associative caches to predict in which Set a block resides. If correctly predicted Hit time is reduced because the signal path to read out the block may be preset for that Set (means selecting entries in the multiplexers). If mispredicted typically a one clock cycle miss penalty is experienced. See text book on page 295 and Lecture 4.
D)

Multibanked Caches:

- Divide cache blocks into banks that can be accessed simultaneously
- While one bank is accessed for possibly several cycles, next access can proceed if it goes to another bank
- Bank is selected based on block address

See as an example fig. 5.6 on page 298.
E) Loop interchange: The compiler interchanges loops so variables are accessed according to their storing order in memory (improving locality). The example below is used when the A matrix is stored in Row major order, i.e. row by row.

## Before:

$$
\begin{gathered}
\text { for (col= } 0 ; \text { col }<\mathrm{N} ; \text { col++) } \\
\text { for (row }=0 ; \text { row }<\mathrm{N} ; \text { row++) } \\
\text { A }[\text { row }, \text { col }]=\ldots
\end{gathered}
$$

After:
for (row = 0 ; row $<\mathrm{N}$; row++)
for ( $\mathrm{col}=0$; $\mathrm{col}<\mathrm{N}$; col++)
$\mathrm{A}[$ row, col] $=$...

See lecture 4 slides p. 40 .

## Assignment 5.

A) Fine-Grain: switch thread on each clock cycle.

Coarse-Grain: switch thread on long latency operation (e.g. cache misses)
B) Instruction Fetch front-ends added per thread and register file structures. May also involve adding more associativety and sizes of cache and TLB structures. And number and size of load/store queues. See example in text book p. 176-177.
C) MIMD = Multiple Instruction Streams Multiple Data Streams. Eaxh processor has its own instruction flow operated on a unique flow om data.
D) All processors need to monitor the addresses sent on the bus. If a write occurs all other processors marks this block as invalid in their cache. On cache misses, a processors holding a dirty copy of the block supplies that block in response to the read request and causes the memory access to be aborted. See textbook on page 208-.

